

tion of  $\Gamma_{\alpha}^{-}$ , and  $V_{\alpha i \beta j}^{-}(r)$  transforms as the product  $q_{\alpha i}^{-} \times q_{\beta j}^{+}$ . In this approach no other terms of the same order in the distortions  $q_{\alpha i}$  contribute to our effects.

The zeroth-order electronic wave function  $\psi_{\mu i}$  is an eigenfunction of  $H_e$ .  $\psi_{\mu i}$  describes the electronic state in the static complex and is the  $i$ -th basis function of the  $\mu$ -th irreducible representation. Taking  $H_{e1}$  as a perturbation and the ionic displacements  $q_{\alpha i}$  as parameters, we obtain a mixing between even and odd electronic states  $\psi_{\mu i}$  of the defect:

$$\psi'_{\mu i} = \psi_{\mu i} + \sum_{v,j} \frac{\langle \psi_{v j}^{-} | H_{e1} | \psi_{\mu i}^{+} \rangle}{E_{\mu} - E_v} \psi_{v j}^{-}. \quad (4)$$

The electronic wave functions  $\psi'_{\mu j}(q_{\alpha i})$  and the energies  $E_{\mu j}(q_{\alpha i})$  are now functions of the lattice distortions  $q_{\alpha i}$ . The nuclear wave functions  $\chi_k^{\mu j}(q_{\alpha i})$  are eigenfunctions of  $H_1 + E_{\mu j}(q_{\alpha i})$ , where  $k$  denotes the set of nuclear quantum numbers. The wave functions of the system are products of  $\psi'_{\mu j}$  and  $\chi_k^{\mu j}$  [10]:

$$\Psi_{\mu j}^k = \psi'_{\mu j} \chi_k^{\mu j}. \quad (5)$$

The oscillator strength  $f$  of the electronic dipole transition between the ground state  $\psi_0$  and the excited state  $\psi'_{\mu}$  is given by [10]

$$f_{0\mu} = \frac{2}{3} \frac{m^*}{\hbar^2} \bar{\epsilon}_{0\mu} \text{Av}_0 \sum_i \left| \langle \psi_0 | \sum_{j=1}^Z r_j | \psi'_{\mu i} \rangle \right|^2. \quad (6)$$

$m^*$  denotes the effective mass of the electron,  $\bar{\epsilon}_{0\mu}$  the mean energy of the transition,  $r_j$  the electric dipole operator, and  $\text{Av}_0$  the thermal average over the ground state.

For the present we take only the linear term (3a) of  $H_{e1}$  into account. We insert (4) into (6) and take the thermal average of products of the form  $q_{\alpha i} q_{\beta j}$ . Since we consider static and dynamic distortions of the lattice cell, each ionic displacement  $q_{\alpha i}$  consists of a static part  $Q_{\alpha i 0}$  and a dynamic part  $Q_{\alpha i}$ :

$$q_{\alpha i} = Q_{\alpha i} + Q_{\alpha i 0}. \quad (7)$$

Using the orthogonality of the symmetry coordinates  $q_{\alpha i}$  of the complex we obtain

$$\begin{aligned} \langle q_{\alpha i} q_{\beta j} \rangle &= \langle Q_{\alpha i} Q_{\beta j} + Q_{\alpha i} Q_{\beta j 0} + Q_{\alpha i 0} Q_{\beta j} + Q_{\alpha i 0} Q_{\beta j 0} \rangle = \\ &= \langle Q_{\alpha i} Q_{\beta j} \rangle \delta_{\alpha\beta} \delta_{ij} + Q_{\alpha i 0} Q_{\beta j 0}. \end{aligned} \quad (8)$$

In analogy to the Jahn-Teller effect, the  $Q_{\alpha i 0}$  are the coordinates of the potential minima of the total energy of the complex including the linear electron-lattice interaction, but in contrast to the even-parity Jahn-Teller distortions, we only consider off-centre displacements with odd parity which do not contribute to the energy in first order. In linear approximation only distortions of odd parity contribute to the oscillator strength  $f$  of the transition. The octahedral complex has two threefold odd vibrations of  $\Gamma_4^{-}$ -symmetry and one threefold degenerate odd vibration of  $\Gamma_5^{-}$ -symmetry. Since IR resonance modes were observed in NaCl:Cu<sup>+</sup> and in KCl:Ag<sup>+</sup> we neglect effects from  $\Gamma_5^{-}$ -modes and assume that only one  $\Gamma_4^{-}$ -mode ( $q_{4 i}^{-}$ ) contributes to the parity breaking effect.  $Q_{4 i 0}^{-} = (Q_{4 x 0}^{-}, Q_{4 y 0}^{-}, Q_{4 z 0}^{-})$  is called an off-centre distortion of the defect. We take the average of all the possible off-centre positions in the lattice cell:

$$\begin{aligned} \text{Av(off-centre)} \quad Q_{4 i 0}^{-} Q_{4 j 0}^{-} &= \frac{1}{N_{\text{off-c.}}} \sum Q_{4 i 0}^{-} Q_{4 j 0}^{-} = \\ &= Q_{4 i 0}^2 \delta_{ij} = Q_{4 j 0}^2 \delta_{ij} = \frac{1}{3} Q_0^2 \delta_{ij}. \end{aligned} \quad (9)$$